

- 1 The diagram shows a trapezium $ABCD$ in which AB and DC are parallel.

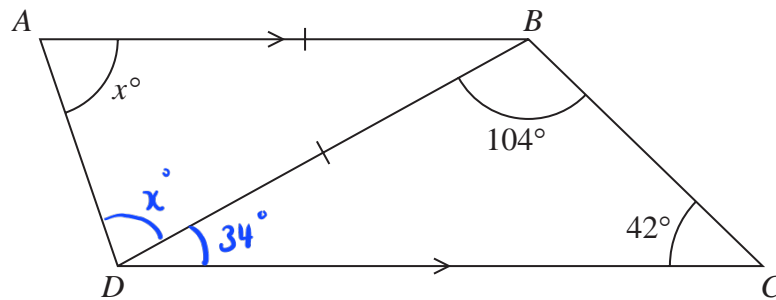


Diagram **NOT**
accurately drawn

$$AB = DB$$

Work out the value of x .

Give a reason for each stage of your working.

$$\begin{aligned} \text{angle } BDC &= 180^\circ - 104^\circ - 42^\circ \\ &= 34^\circ \quad (\text{angle in a triangle sums up to } 180^\circ) \end{aligned}$$

$$\text{angle } BAD = \text{angle } ADB = x^\circ \quad (\text{because } ABD \text{ is an isosceles triangle})$$

$$\text{angle } BAD = 180^\circ - x^\circ - 34^\circ \quad (\text{because co-interior angle adds up to } 180^\circ)$$

$$x^\circ = 180^\circ - x^\circ - 34^\circ$$

$$2x^\circ = 146^\circ$$

$$x^\circ = 73^\circ$$

$$x = 73$$

(Total for Question 1 is 4 marks)

2

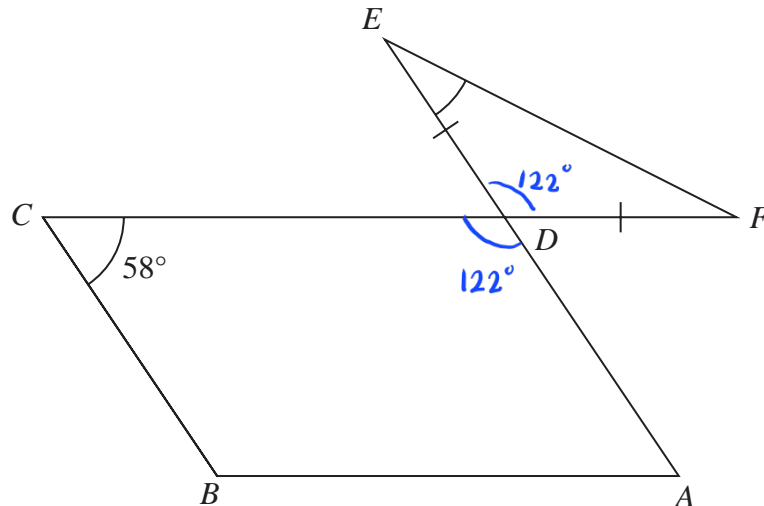


Diagram **NOT**
accurately drawn

The diagram shows a parallelogram $ABCD$ and an isosceles triangle DEF in which $DE = DF$

CDF and ADE are straight lines.

Angle $BCD = 58^\circ$

Work out the size of angle DEF .

Give a reason for each stage of your working.

$$\text{angle } ADC = 180^\circ - 58^\circ$$

$$= 122^\circ \quad (1)$$

(co-interior angles add up to 180°) (1)

$$\text{angle } EDF = \text{angle } ADC = 122^\circ$$

(vertically opposite angles are equal)

$$\text{angle } DEF = \frac{180^\circ - 122^\circ}{2} = \frac{58^\circ}{2} \quad \leftarrow \text{(base angles in isosceles are the same)}$$

$$= 29^\circ \quad (1)$$

(angles in triangle add up to 180°) (1)

3

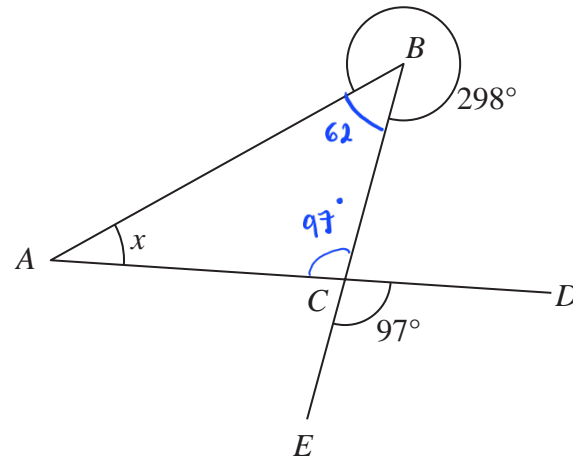


Diagram **NOT**
accurately drawn

ABC is a triangle.

D and E are points such that ACD and BCE are straight lines.

reflex angle $ABC = 298^\circ$

angle $ECD = 97^\circ$

Work out the size of angle x .

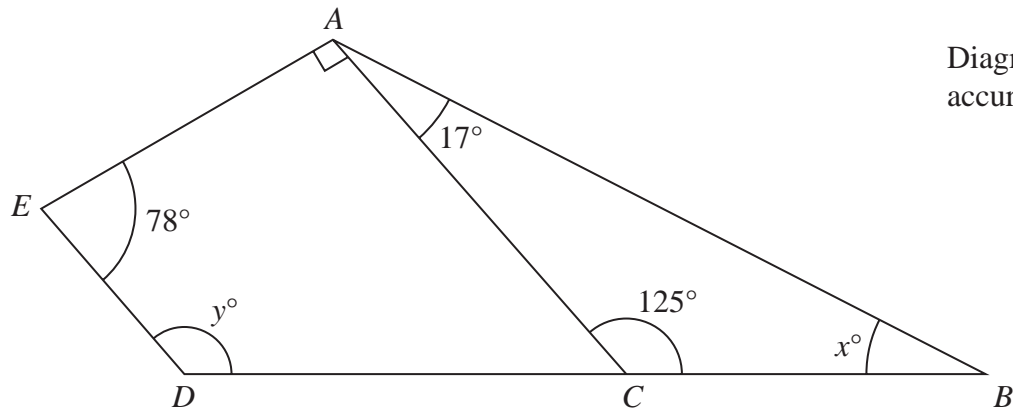
Give a reason for each stage of your working.

- angle $ACB = \text{angle } ECD = 97^\circ$ ①
(vertically opposite angles are equal) ①
- angle $ABC = 360^\circ - 298^\circ$
 $= 62^\circ$
(angles around a point adds up to 360°) ①
- $x = 180^\circ - 62^\circ - 97^\circ$
 $= 21^\circ$ ①
(angles in a triangle sums up to 180°)

$x = 21^\circ$

(Total for Question 3 is 4 marks)

4

Diagram **NOT**
accurately drawn

$ABDE$ is a quadrilateral.
 ABC is a triangle.
 DCB is a straight line.

(a) (i) Work out the value of x .

$$\begin{aligned} x &= 180^\circ - 125^\circ - 17^\circ \\ &= 38^\circ \quad (1) \end{aligned}$$

$$x = \underline{\quad 38 \quad} \quad (1)$$

(ii) Give a reason for your answer.

Angles in a triangle sums up to 180° (1)

(1)

(b) Work out the value of y .

Give a reason for each stage of your working.

$$\begin{aligned} \text{angle } ACD &= 180^\circ - 125^\circ \quad (1) \\ &= 55^\circ \quad (\text{angles on a straight line add up to } 180^\circ) \end{aligned}$$

$$\begin{aligned} y^\circ &= 360^\circ - 78^\circ - 90^\circ - 55^\circ \quad (1) \\ &= 137^\circ \quad (1) \\ &\quad (\text{angles in a quadrilateral add up to } 360^\circ) \end{aligned}$$

$$y = \underline{\quad 137 \quad} \quad (3)$$

(Total for Question 4 is 5 marks)

- 5 The diagram shows a square $ABCD$ and a regular pentagon $CDEFG$.

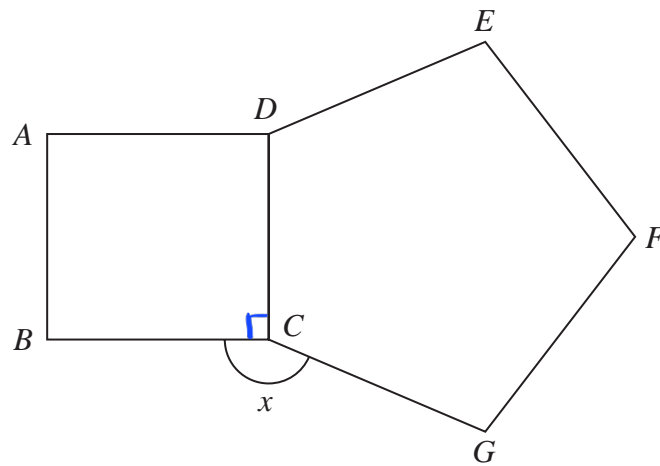


Diagram **NOT**
accurately drawn

Work out the size of the angle marked x .

$$\text{angle } DCB = 90^\circ$$

$$\begin{aligned} \text{angle } DCG &= \frac{5-2}{5} \times 180^\circ - \text{interior angle of a pentagon} \\ &= 108^\circ \text{ (1)} \end{aligned}$$

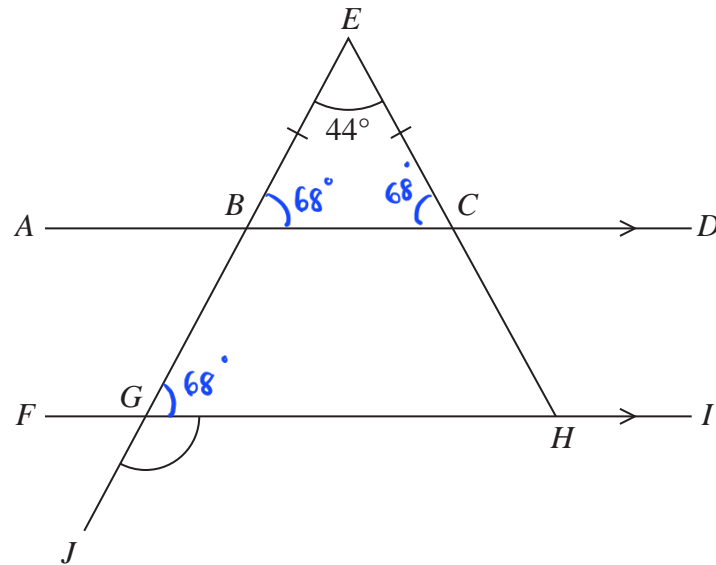
$$\begin{aligned} \text{angle } BCG &= 360^\circ - 90^\circ - 108^\circ \text{ (1)} \\ &= 162^\circ \text{ (1)} \end{aligned}$$

162

o

(Total for Question 5 is 3 marks)

6

Diagram **NOT**
accurately drawn

$ABCD$ and $FGHI$ are parallel straight lines.
 $EBGJ$ and ECH are straight lines.

$$BE = CE$$

$$\text{Angle } BEC = 44^\circ$$

Work out the size of angle JGH .

Give a reason for each stage of your working.

$$\text{angle } EBC = \frac{180^\circ - 44^\circ}{2} = 68^\circ \quad (1)$$

(angles at the base of isosceles triangle are the same)

$$\text{Angle } BGH = \text{angle } EBC = 68^\circ \quad (1)$$

(corresponding angles are the same) (1)

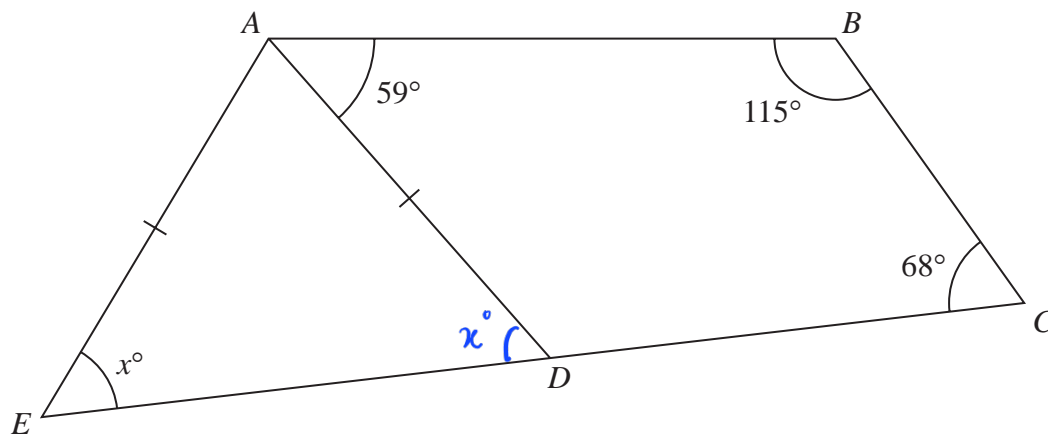
$$\text{angle } JGH = 180^\circ - 68^\circ = 112^\circ \quad (1)$$

(angles on a straight line sum up to 180°) (1)

12

(Total for Question 6 is 5 marks)

- 7 The diagram shows quadrilateral $ABCD$ and isosceles triangle ADE , where $AE = AD$.



EDC is a straight line.

Work out the value of x .

Give a reason for each stage of your working.

$$\angle ADE = x^\circ$$

(the base angles of an isosceles triangle are equal)

$$\begin{aligned}\angle ADC &= 360^\circ - 115^\circ - 68^\circ - 59^\circ \\ &= 118^\circ \text{ (1)}\end{aligned}$$

(angles in a quadrilateral sum up to 360°) (2)

$$\begin{aligned}\angle ADE &= 180^\circ - 118^\circ \\ &= 62^\circ \text{ (1)}\end{aligned}$$

(angles on a straight line sum up to 180°)

$$x = 62^\circ$$

(Total for Question 7 is 4 marks)

8

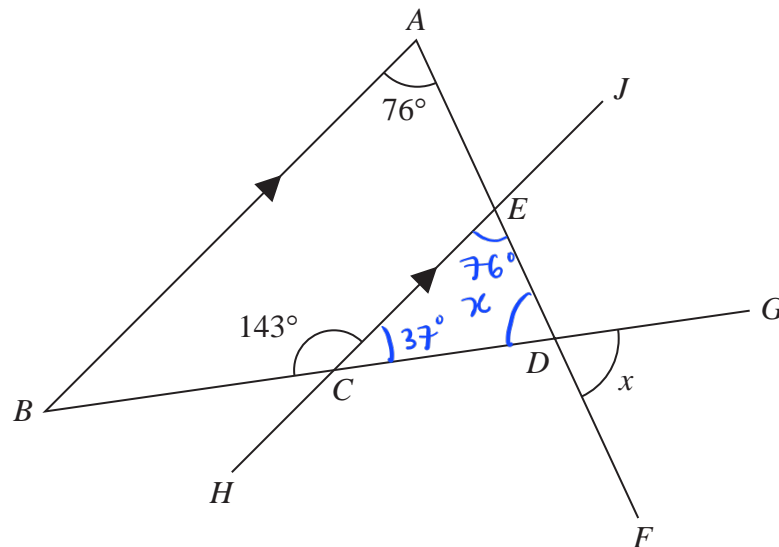


Diagram **NOT**
accurately drawn

ABD is a triangle.

$AEDF$, $BCDG$ and $HCEJ$ are straight lines.

BA is parallel to $HCEJ$.

Work out the size of the angle marked x .

$$\angle ECD = 180^\circ - 143^\circ = 37^\circ \quad (1)$$

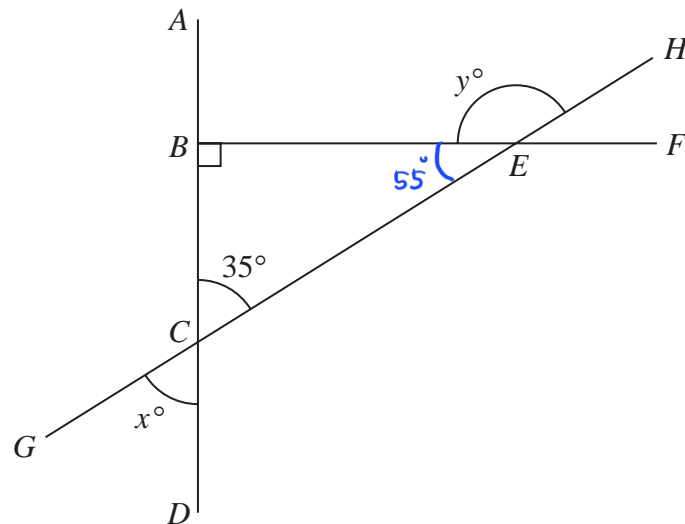
$$x = 180^\circ - 76^\circ - 37^\circ = 67^\circ$$

(1) (1)

67 °

(Total for Question 8 is 3 marks)

9

Diagram **NOT**
accurately drawn

In the diagram, BCE is a right-angled triangle.
 $ABCD$, BEF and $GCEH$ are straight lines.

Angle $BCE = 35^\circ$

(a) (i) Find the value of x

$$x^\circ = \text{angle } BCE = 35^\circ \quad (1)$$

$$x = \underline{\hspace{2cm} 35 \hspace{2cm}} \quad (1)$$

(ii) Give a reason for your answer.

Vertically opposite angles are equal. (1)

(1)

(b) (i) Work out the value of y

$$\begin{aligned} \text{angle } BEC &= 180^\circ - 35^\circ - 90^\circ \\ &= 55^\circ \quad (1) \end{aligned}$$

$$\begin{aligned} y^\circ &= 180^\circ - 55^\circ \\ &= 125^\circ \quad (1) \end{aligned}$$

$$y = \underline{\hspace{2cm} 125 \hspace{2cm}} \quad (2)$$

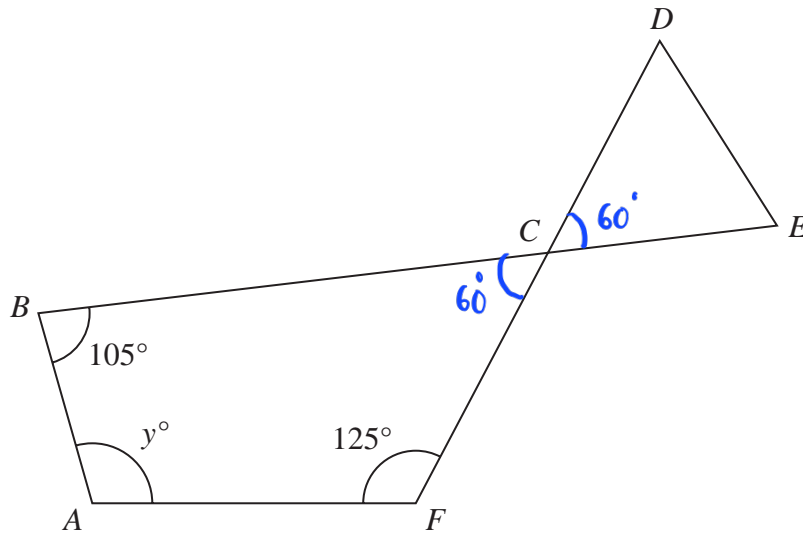
(ii) Give a reason for your answer.

Angles in a triangle add up to 180° . Angles on a straight line add up to 180° . (1)

(1)

(Total for Question 9 is 5 marks)

10

Diagram **NOT**
accurately drawn

CDE is an equilateral triangle.
 $ABCF$ is a quadrilateral.

BCE and DCF are straight lines.

- (b) Work out the value of y
 You must show your working.

$$\begin{aligned} CDE &: 180^\circ \div 3 \\ &= 60^\circ \text{ each angle } \textcircled{1} \end{aligned}$$

$$\begin{aligned} y^\circ &= 360^\circ - (105^\circ + 125^\circ + 60^\circ) \textcircled{1} \\ &= 360^\circ - 290^\circ \\ &= 70^\circ \textcircled{1} \end{aligned}$$

$$y = \overset{70}{\dots\dots\dots} \textcircled{3}$$

(Total for Question 10 is 3 marks)

11 ABC is a straight line and BCD is a triangle.

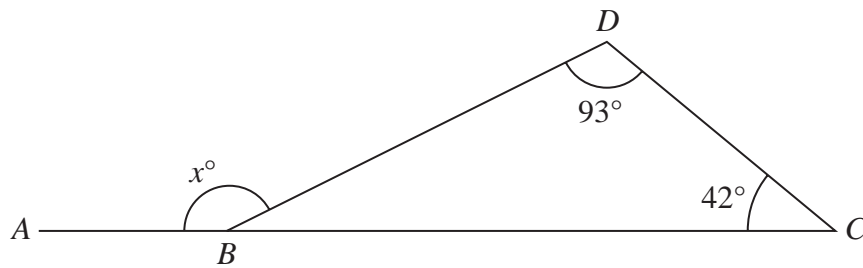


Diagram **NOT**
accurately drawn

(a) Work out the value of x

$$\begin{aligned} x &= 180^\circ - (180^\circ - 93^\circ - 42^\circ) \quad (1) \\ &= 93^\circ + 42^\circ \\ &= 135^\circ \quad (1) \end{aligned}$$

$$x = \frac{135}{(2)}$$

PO , RO , SO and TO are four straight lines.

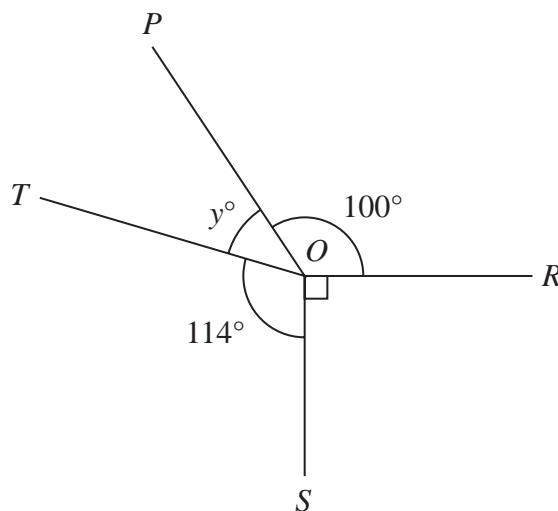


Diagram **NOT**
accurately drawn

(b) (i) Work out the value of y

$$\begin{aligned} y &= 360^\circ - 100^\circ - 114^\circ - 90^\circ \quad (1) \\ &= 56^\circ \quad (1) \end{aligned}$$

$$y = \frac{56}{(2)}$$

(ii) Give a reason for your answer.

Angles at a point sum up to 360° . (1)

(1)

(Total for Question 11 is 5 marks)

12 The diagram shows triangle ABD

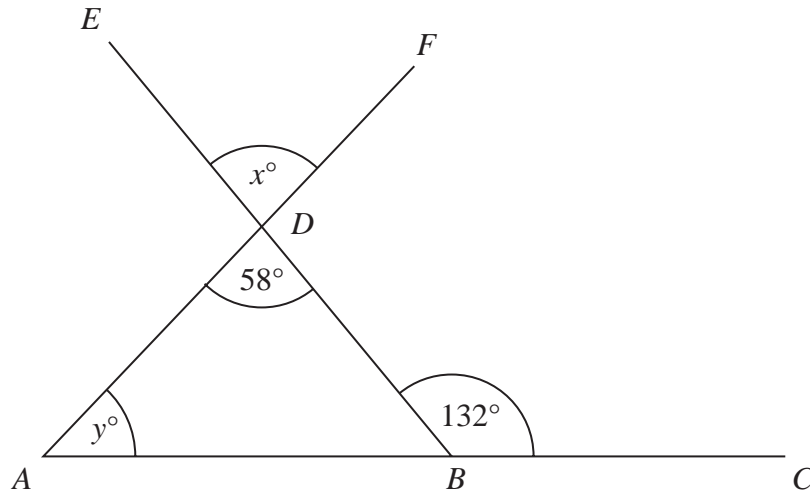


Diagram **NOT**
accurately drawn

ABC , BDE and ADF are straight lines.

angle $CBD = 132^\circ$ angle $ADB = 58^\circ$

(a) (i) Write down the value of x

$x = 58^\circ$ (1)

(ii) Give a reason for your answer.

Vertically opposite angles are equal (1)

(2)

(b) Work out the value of y

$$\begin{aligned} \angle ABD &= 180^\circ - 132^\circ \\ &= 48^\circ \end{aligned} \quad (1)$$

$$\begin{aligned} y^\circ &= 180^\circ - 58^\circ - 48^\circ \\ &= 74^\circ \end{aligned} \quad (1)$$

$y = 74^\circ$
(2)

(Total for Question 12 is 4 marks)

13

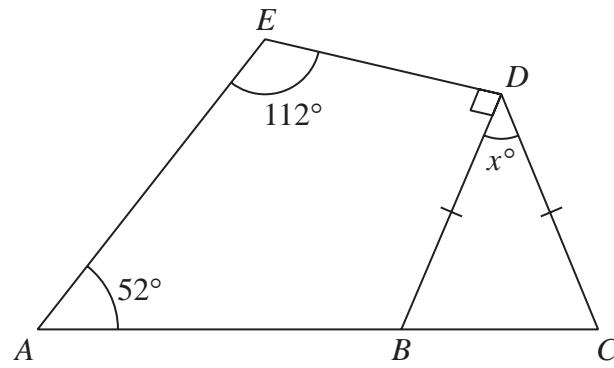


Diagram **NOT**
accurately drawn

BCD is an isosceles triangle with $BD = CD$

ABC is a straight line.

$ABDE$ is a quadrilateral.

Work out the value of x

Give a reason for each stage of your working.

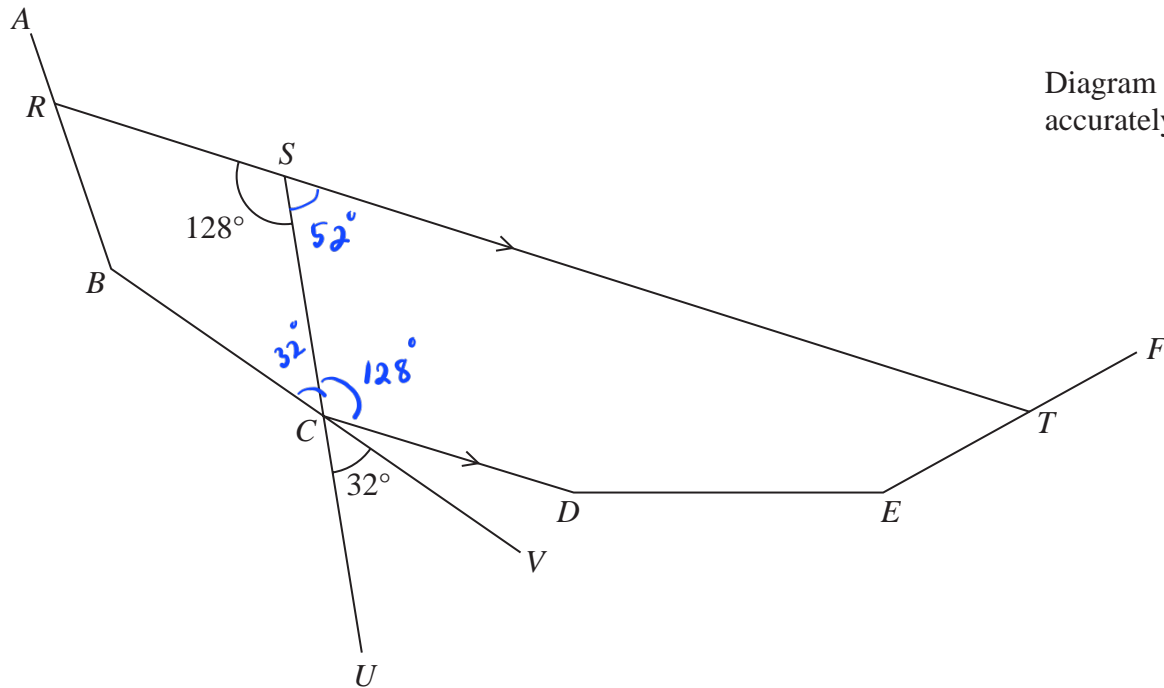
$$\begin{aligned}
 \angle BDE &= 360 - 52 - 112 - 90 \\
 &= 106 \quad (1) \\
 &\quad (\text{angles in a quadrilateral add up to } 360^\circ) \quad (1) \\
 \angle CBD &= 180 - 106 \\
 &= 74 \quad (1) \\
 &\quad (\text{angles on a straight line add to } 180^\circ)
 \end{aligned}$$

$$\begin{aligned}
 x &= 180^\circ - 2(74^\circ) \quad - (\text{base angles in isosceles are equal}) \\
 &= 180^\circ - 148^\circ \\
 &= 32^\circ \quad (1)
 \end{aligned}$$

$$x = \text{32}$$

(Total for Question 13 is 4 marks)

14

Diagram **NOT**
accurately drawn

AB , BC , CD , DE and EF are five sides of a regular polygon.

RST , SCU and BCV are straight lines.

RST is parallel to CD

Angle $RSC = 128^\circ$

Angle $UCV = 32^\circ$

Work out how many sides the polygon has.

Show your working clearly.

$$\angle BCS = \angle UCV = 32^\circ$$

$$\angle SCD = \angle RSC = 128^\circ \quad (1)$$

$$\angle TSC = 180^\circ - 128^\circ = 52^\circ$$

$$\text{interior angle} = 128^\circ + 32^\circ = 160^\circ \quad (1)$$

$$180(n-2) = 160n \quad (1)$$

$$180n - 360 = 160n$$

$$20n = 360$$

$$n = 18 \quad (1)$$

18

(Total for Question 14 is 4 marks)

15 The diagram shows a pentagon.

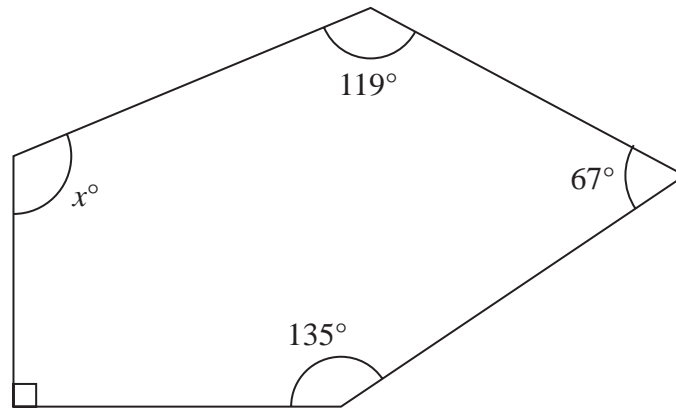


Diagram **NOT**
accurately drawn

Work out the value of x

$$\text{Total angle : } 3 \times 180^\circ = 540^\circ \quad (1)$$

$$540 - 90 - 135 - 67 - 119 \quad (1)$$

$$= 540 - 411$$

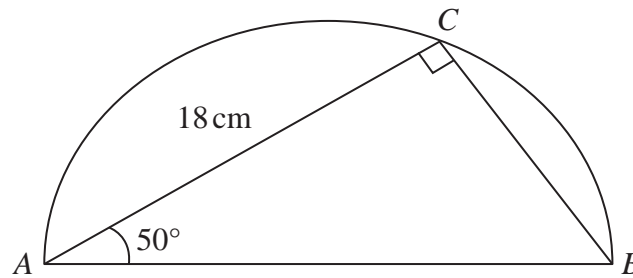
$$= 129 \quad (1)$$

$$x = 129$$

(Total for Question 15 is 3 marks)

16 The diagram shows a triangle ABC inside a semicircle.

Diagram **NOT**
accurately drawn



A , B and C are points on the semicircle.

AB is the diameter of the semicircle.

Angle $ACB = 90^\circ$

Angle $BAC = 50^\circ$

$AC = 18 \text{ cm}$

Work out the perimeter of the semicircle.

Give your answer correct to 2 significant figures.

$$\cos 50^\circ = \frac{18}{AB} \quad (1)$$

$$AB = \frac{18}{\cos 50^\circ} \quad (1)$$

$$= 28.0030 \dots$$

$$\frac{1}{2} \times \pi \times 28.0030 \dots = 43.9 \dots \quad (1)$$

$$28.0030 \dots + 43.9 \dots \quad (1)$$

$$= 71.9900 \dots$$

$$\approx 72 \quad (1)$$

72

..... cm

(Total for Question 16 is 5 marks)

17 The diagram shows two parallel lines AB and DEF

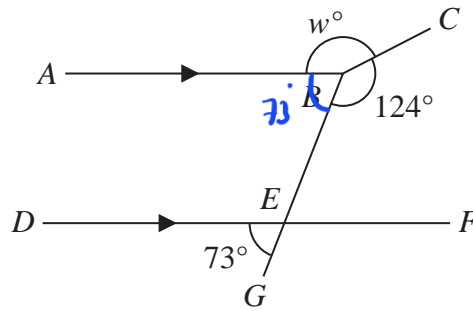


Diagram **NOT**
accurately drawn

BEG is a straight line.

$$\text{angle } DEG = 73^\circ \quad \text{angle } EBC = 124^\circ \quad \text{angle } ABC = w^\circ$$

Work out the value of w

Give reasons for each stage of your working.

$$\text{angle } ABE = \text{angle } DEG = 73^\circ \quad (1)$$

(corresponding angles are equal) (1)

$$w = 360^\circ - 124^\circ - 73^\circ \quad (1)$$

$$= 163^\circ \quad (1)$$

(angles at a point add up to 360°)

163

$w = \dots\dots\dots$

(Total for Question 17 is 4 marks)

18 The diagram shows quadrilateral $ABCD$

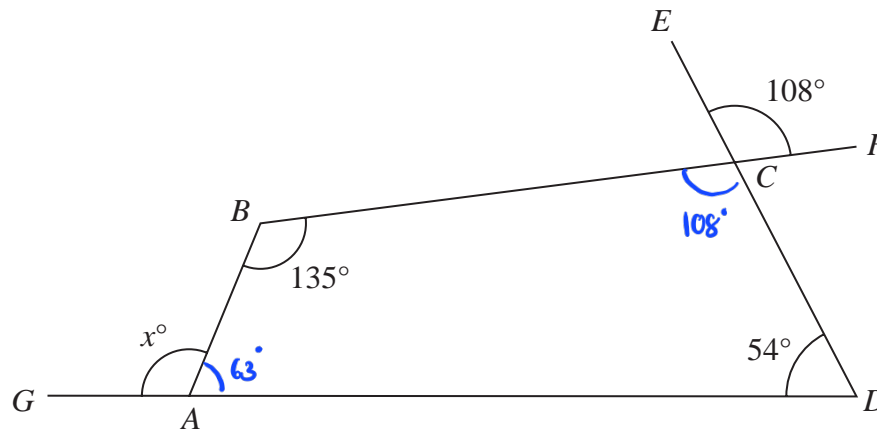


Diagram **NOT** accurately drawn

ECD , BCF and GAD are straight lines.

Work out the value of x

Give a reason for each stage of your working.

$$\text{angle } BCD = \text{angle } ECF = 108^\circ \quad (1)$$

(vertically opposite angles are equal)

$$\text{angle } BAD = 360^\circ - 135^\circ - 108^\circ - 54^\circ = 63^\circ \quad (1)$$

(angles in a quadrilateral add up to 360°) (1)

$$x^\circ = 180^\circ - 63^\circ$$

$$= 117^\circ \quad (1)$$

(angles on a straight line add up to 180°) (1)

$$x = \underline{\quad 117 \quad}$$

(Total for Question 18 is 5 marks)

19 The diagram shows quadrilateral $ABCD$

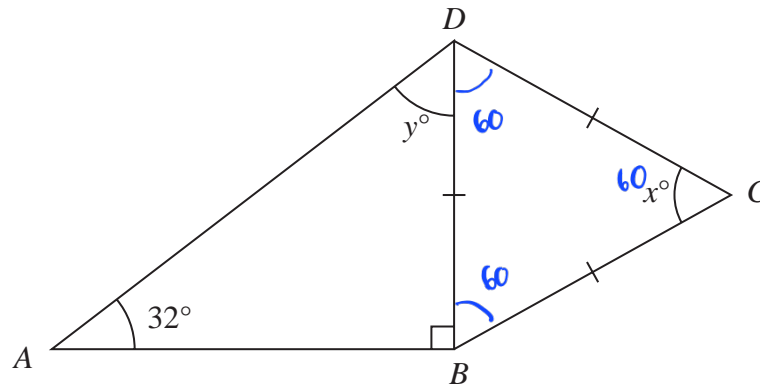


Diagram **NOT**
accurately drawn

$$BC = CD = DB$$

angle $DBA = 90^\circ$ and angle $DAB = 32^\circ$

(a) Work out the value of x

$$x = \frac{60}{1} \quad (1)$$

(b) (i) Work out the value of y

$$180 - 90 - 32 = 58$$

$$y = \frac{58}{1} \quad (1)$$

(ii) Give a reason for your answer to (b)(i).

Angles in a triangle add up to 180° (1)

(1)

(Total for Question 19 is 3 marks)

20 $ABCD$ is a trapezium.

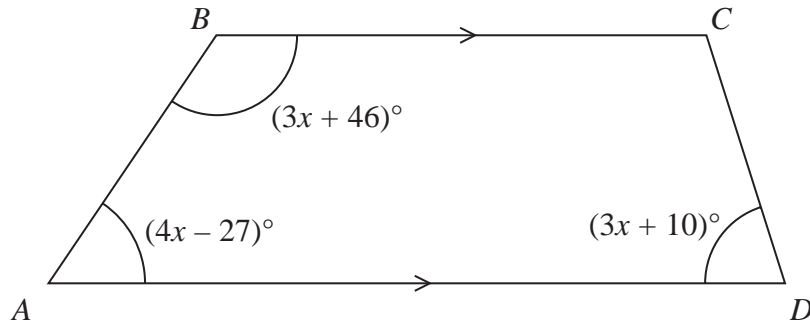


Diagram **NOT**
accurately drawn

BC is parallel to AD

Find the size of the largest angle inside the trapezium.

$$(4x - 27) + (3x + 46) = 180 \quad (1)$$

$$7x = 180 - 19$$

$$7x = 161$$

$$x = 23 \quad (1)$$

$$ABC = 3(23) + 46 = 115$$

$$BAD = 4(23) - 27 = 65 \quad (1)$$

$$ADC = 3(23) + 10 = 79$$

$$BCD = 180 - 79 = 101$$

(1) 115

(Total for Question 20 is 4 marks)

21 Here is a 9-sided regular polygon $ABCDEFGHIJ$, with centre O

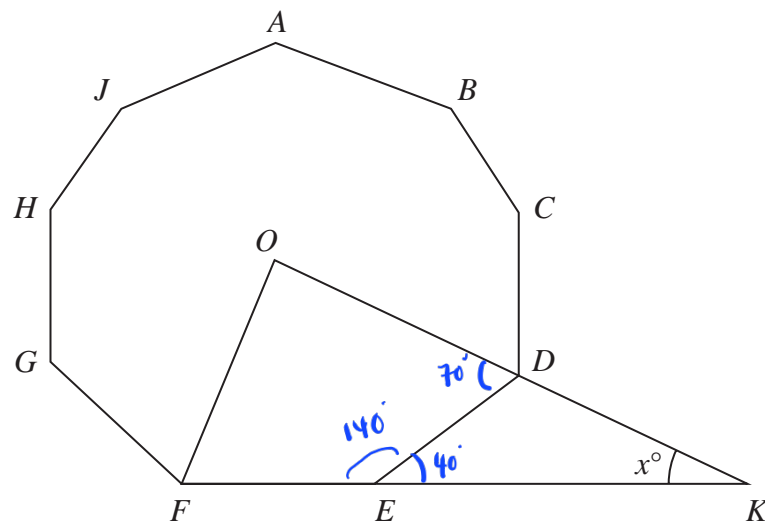


Diagram **NOT**
accurately drawn

ODK and FEK are straight lines.

Work out the value of x

$$\text{interior angle of polygon} = \frac{(9-2)(180)}{9} = 140^\circ \quad (1)$$

$$DEK = 180^\circ - 140^\circ = 40^\circ$$

$$EDK = 180^\circ - \left(\frac{140}{2}\right) = 110^\circ \quad (1)$$

$$x = 180^\circ - 110^\circ - 40^\circ$$

$$= 30^\circ \quad (1)$$

$$x = \underline{\quad 30 \quad}$$

(Total for Question 21 is 3 marks)